One of the great advantages of formal semantics is that we can actually prove that a program will behave correctly for *all* expected input values.

In order for this to work we need the notion of a *program specification*.

The program specification act as the *yard stick* for the expected program behavior for any set of input values.
A program specification is a universally quantified sentence over states in first order logic.

Consider the following program specification for some program $p$ and variables $x$ and $y$:

$$\forall s, \exists P, Q, VX, VY \ [(P, s) \rightarrow Q \land$$
$$\text{lookup}(y, s, VY) \land \text{lookup}(x, Q, VY) \land$$
$$\text{lookup}(x, s, VX) \land \text{lookup}(y, Q, VX)]$$

This specification states that running the program $P$ in state $s$ will give rise to some state $Q$. Furthermore, looking up the variable $y$ in state $s$ is the same as looking up the variable $x$ in state $Q$ and vice versa.

This is a program specification for a swap program that swaps the values of $x$ and $y$. 
Now, consider the program $P$ written in our simple language IMP defined in ‘sem.pl’:

$$P \equiv \text{assign}(t, x) \text{ seq assign}(x, y) \text{ seq assign}(y, t)$$

Without formal semantics and a program specification we would simply try “a bunch” of values, and if the results look good we would infer that the program works. But there will always be a doubt that it will work for all states since trying a bunch of values does not constitute a proof.

However, given our formal semantics we can prove that this program satisfies the specification and therefore we can prove that the program works for all possible states.
%% swap.pl
:- ['sem.pl'].

:- >>> 'show that program P="assign(t,x) seq assign(x,y) seq assign(y,t))"'.
:- >>> 'satisfies the program specification:'.
:- >>> '(P,s) -->> Q, lookup(y,s,VY), lookup(x,Q,VY), lookup(x,s,VX), lookup(y,Q,VX)'.

program(assign(t,x) seq assign(x,y) seq assign(y,t)).

:- asserta(lookup(x,s,vx)).
:- asserta(lookup(y,s,vy)).

:- program(P),
   (P,s) -->> Q,
   lookup(y,s,VY),
   lookup(x,Q,VY),
   lookup(x,s,VX),
   lookup(y,Q,VX).
Now consider the program specification

$$\forall s, \exists P, Q, V_1, V_2 \quad \left[(P, s) \implies Q \land \text{lookup}(z, s, V_1) \land \text{lookup}(z, Q, V_2) \land V_2 = 2 \times V_1\right]$$

It is easy to see that the program $P \equiv \text{assign}(z, \text{mult}(2, z))$ satisfies the specification.

But so does this program $P \equiv \text{assign}(z, \text{add}(z, z))$.

$\Rightarrow$ Program specifications are *implementation independent*!
% double.pl
:-['sem.pl'].

:- >>> 'show that program P="assign(z,add(z,z))"'.
:- >>> 'satisfies the program specification:'.
:- >>> ' (P,s) -->> Q,lookup(z,s,V1),lookup(z,Q,V2),V2 = 2*V1'.

program(assign(z,add(z,z))).

:- asserta(lookup(z,s,vz)).
:- asserta(2*I xis I+I). % property of integers

:- program(P),
   (P,s) -->> Q,
   lookup(z,s,V1),
   lookup(z,Q,V2),
   V2 = 2 * V1.