

#### Higher-Order Programming: The Essence of Functional Programming

 Higher-Order programming is defined as

 Programming with functions as arguments to other functions or functions as return values from functions.



#### Higher-Order Programming: A Cornerstone of Functional Programming

- It is a natural outgrowth from the lambda calculus where
  - a) lambda expressions can be passed to other lambda expressions, and
  - b) new lambda expressions can be computed by lambda expressions

• **E.g.** 

a) 
$$(\lambda y. y 1)(\lambda x. x + 1) \Rightarrow 2$$

b)  $(\lambda x. (\lambda y. x + y)) 1 1 \Rightarrow 2$ 

## Modifying Behavior of aFunction

- We can use this to write generic functions which we can then make specific by passing in desired behavior via a function.
- Note: this is NOT programming with generics
  - Generics are generic with respect to types
  - Higher-order functions are generic with respect to behavior!

# Image: Modifying Behavior of aFunction

### • The 'filter' function is generic with regards to the ordering predicate



If e is kept or discarded depends on the passed in function – the filter function has a generic filtering capability which is made specific by the passed in predicate.

## Modifying Behavior of a Function - QuickSort



## Kolomotic Modifying Behavior of a Function

 The Asteroid sort module is another example, sort @sort (p:%function, I:%list)





### **Dispatch Tables**

- We can also associate behavior with appropriate keys in a dispatch table.
- We can then dispatch (lookup) desired behavior given specific keys.
- Example: A generic 'calculate' function that takes two values and a key symbol and then performs the appropriate computation.



### **Dispatch Tables**

```
load system hash.
 1
 2
      let dispatch_table = hash @hash ().
 3
 4
 5
     dispatch_table @insert [
         ("+", lambda with (a,b) do a + b),
 6
         ("-", lambda with (a,b) do a - b),
 7
         ("*", lambda with (a, b) do a * b),
 8
         ("/",lambda with (a,b) do a / b)
 9
      1
10
11
12
      function calculate with (operator, a, b) do
         dispatch_table @get operator (a,b)
13
     end
14
15
     -- Example usage
16
17
      assert (calculate("+", 3, 5) == 8)
      assert (calculate("-", 7, 2) == 5)
18
      assert (calculate("*", 2, 4) == 8)
19
      assert (calculate("/", 10, 2) == 5)
20
```

In012/dispatch2.ast



### Map & Reduce

- The 'map' and 'reduce' functions are functions that take a function and apply the given function to ALL the elements of a list.
- Both functions are higher-order functions that come straight out of the functional programming tradition.



- Below is Asteroid code that explains the behavior of the map function.
- Beware that map is not required to apply the function f in the sequential manner shown here
  - For example, it is free to exploit threads to apply the function f in parallel to the elements of the list.

```
list @map f
-- is equivalent to --
let r = [].
for e in list do
  r @append(f e).
end
let list = r.
```

The function argument to f must be of the same type as the list elements



- One interesting application of map is the transformation of a simple list constructor into any kind of list
  - Here we compute a list of alternating 1's and -1's.

```
1 load system math.
2
3 let a = [1 to 10] @map(lambda with x do math @mod (x,2))
4 | | | | @map(lambda with x do 1 if x else -1).
5 |
6 assert (a == [1,-1,1,-1,1,-1,1,-1]).
```

In012/map.ast



 Most modern languages support some form of 'map' since it is such a powerful programming tool.

#### Python

```
1 l = [x for x in range(1,10+1)]
2 it = map(lambda x : x % 2, l)
3 a = list(map(lambda x : 1 if x else -1, it))
4
5 assert(a == [1,-1,1,-1,1,-1,1,-1])
```

#### Rust

use std::vec::Vec; 1 2 3 fn main() { 4 let a : Vec<i32> = vec! [1,2,3,4,5,6,7,8,9,10] .iter() 5 .map(|x| x % 2) 6 7  $map(|x| \text{ if } x == 0 \{ -1 \} \text{ else } \{ 1 \})$ .collect(); 8 In012/map.rs 9 assert eq!(a, vec![1, -1, 1, -1, 1, -1, 1, -1, 1, -1]); 10 11

In012/map.py



 Whereas 'map' applies a function to a list producing another list, the 'reduce' function applies a function to a list so that the list gets *reduced* to a single value.

 In functional languages this is often called 'fold' – folding the list into a single value



#### For example, the reduce function lets us sum the elements of a list without a loop



The argument of the reduce function must be a pair where each component of the pair is of the element type of the list.



#### The reduce function gives us an interesting way to implement the factorial of an integer



```
1 -- factorial with reduce
2 function fact with x do
3 [1 to x] @reduce (lambda with (i,j) do i*j)
4 end
5
6 assert (fact 3 == 6).
```



- The Asteroid code below illustrates the behavior of the 'reduce' function
  - Notice the function application to a pair of values!
  - The **first value of the pair acts like an accumulator** containing the partially reduced value at each function application
    - In the default setting it is initialized to the first element of the list.

```
list @ reduce f
1
2
    -- is equivalent to --
3
4
    let value = list@0.
5
     for i in range(len(list)) do
6
           let value = f (value,l@i).
7
8
    end
     -- value has now the reduced value of the list
9
```



#### Python



In012/reduce.py



In012/reduce.rs

1	fn main() {	
2	<pre>let value: i32 = (110).reduce( acc, e  acc)</pre>	<pre>cc + e).unwrap();</pre>
3	<pre>assert_eq!(value, 45);</pre>	
4	}	