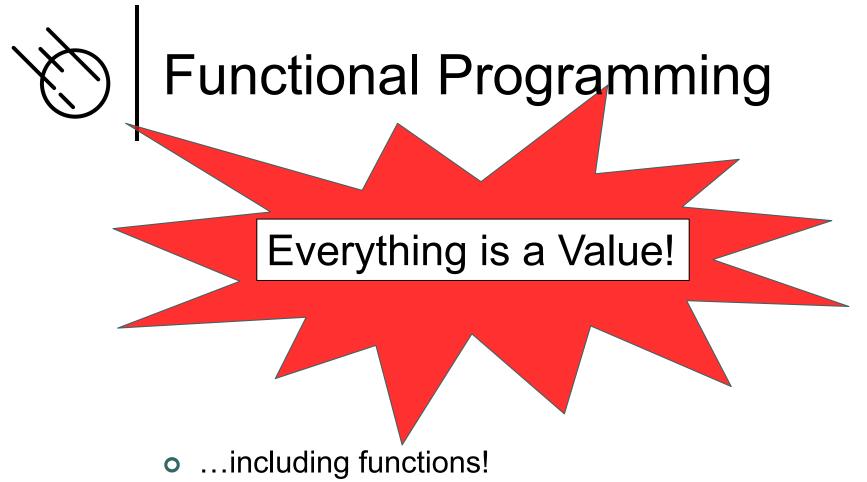


Functional Programming

- Functional programming is a declarative programming paradigm where programs are constructed by applying and composing functions.
- Function definitions are **expressions that map values to other values**, rather than a sequence of imperative statements which update the running state of a program.

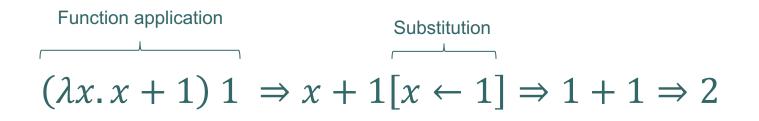


• This sets functional programming apart from imperative programming where statements like loops and conditionals do not represent values but change of an explicit machine state



Lambda Calculus

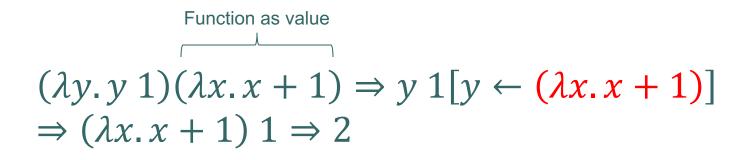
- Let's explore this using the lambda calculus before we commit to any particular language.
- Recall that in the lambda calculus we construct functions as lambda expressions and these functions can be applied to values, e.g.

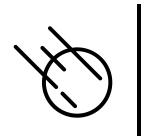




Lambda Calculus

 Functions can be input values to other functions!





Lambda Calculus

 Functions as return values from functions

 That is, functions computing new functions!

Function as return value $\left(\lambda x. (\lambda y. x + y) \right) 1 1 \Rightarrow (\lambda y. x + y) 1[x \leftarrow 1]$ $\Rightarrow (\lambda y. 1 + y) 1 \Rightarrow 1 + y[y \leftarrow 1] \Rightarrow 1 + 1 \Rightarrow 2$



Functional Programming

- Functional programming is declarative in that the programs deal more with the **what** rather than the **how**.
- One way to think about this is: in declarative programming we "declare" what to do for each input configuration.
- This is in stark contrast to imperative programming where we describe **how to solve the whole problem** in one go without subdivision.

```
-- imperative solution
function len with list do
   let remaining_list = list.
   let cnt = 0.
   repeat
      let [_|remaining_list] = remaining_list.
      let cnt = cnt + 1.
   until remaining_list is [].
end
let q = [ 1 to 10].
assert (len q == 10).
```

<pre> declarative solution function len</pre>
with [] do
<pre>with [_ remaining_list] do 1 + len remaining list</pre>
end
let q = [1 to 10]. assert (len q == 10).

"The How"

"The What"





Dr John McCarthy, computer scientist, 1927 – 2011.

- Lisp was developed by John McCarthy in the late 1950's early 60's to solve problems in Al.
- It is the oldest functional programming language.
- Its syntax has been inspired by the lambda calculus.
- It introduced novel features such as recursion and garbage collection.
- It is still in use today as Common Lisp (ANSI compliant).
- Modern descendants: Scheme, Racket, Clojure



$(\lambda x. (\lambda y. x + y))$ 1 1 \Rightarrow 2

[1]> (apply (apply (lambda (x) (lambda (y) (+ x y))) '(1)) '(1))
2
[2]>





Robin Milner, computer scientist 1934 – 2010.



- Robin Milner designed ML as the implementation language for his proof assistant LCF (Logic for Computable Functions) in the 1970's.
- It can be considered the first modern functional programming language,
 - Statically type checked
 - A syntax that is easily recognized by today's developers
 - Very influential, virtually every modern functional programming language can trace its ancestry back to ML
- It is also one of the few high-level programming languages with a full mathematical specification.
- Dialects of ML in wide use today: SMLNJ, Ocaml, F#

https://smlnj.org/ and https://en.wikipedia.org/wiki/ML_(programming_language)



- (fn y => y 1)(fn x => x+1); val it = 2 : int -

 $(\lambda x. (\lambda y. x + y)) 1 1 \Rightarrow 2$ - (fn x => (fn y => x+y)) 1 1;

val it = 2 : int

Standard ML of New Jersey (64-bit) v110.95 [built: Sun Nov 06 00:04:31 2022] - fun inc x = x+1; val inc = fn : int -> int - inc 1; val it = 2 : int -



A Type is a Set of Values.

• If we view functions as values, then they have to belong to a type.

- (fn x => 2*x);

val it = fn : int -> int

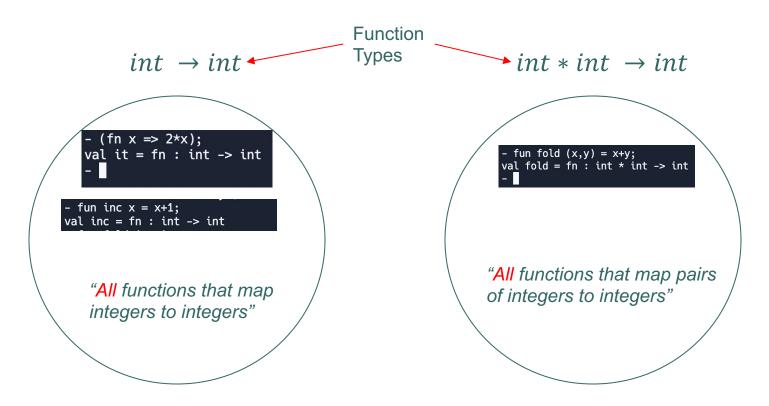
• We can use ML's type system to compute the function types,

- fun inc x = x+1; / val inc = fn : int -> int

- fun fold (x,y) = x+y; val fold = fn : int * int -> int -

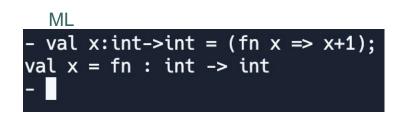


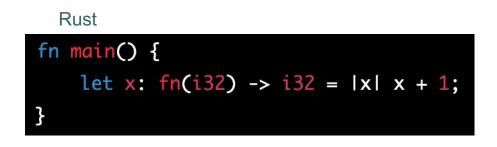
 In the previous slide we saw that we have at least two different types





• Since we now have function types we can declare variables of that type,





Function as Values: Another Look

- Every function belongs to a particular function type.
- We can view a function as a value in the set of all values of a particular type.
- This particularly visible in statically typed languages like ML and Rust.
 - But it is also supported in dynamically typed languages like Python and Asteroid.
 - In Asteroid, all functions are members of the type 'function'.

```
Asteroid Version 1.1.4

(c) University of Rhode Island

Type "asteroid -h" for help

Press CTRL-D to exit

[ast> load system type.

[ast> type @gettype (lambda with x do x+1).

function

[ast> let x:%function = (lambda with x do x+1).

[ast> x

(function ...)

ast>
```



Please read Chapter I in the following paper,

lutzhamel.github.io/CSC493/docs/intro-fp-barendregt.pdf