# Defining Language TWO

- Extend Language ONE with:
  - Variables
  - let expression for assigning values to them



#### Section 23.3

## TWO: Syntax

# TWO: <exp>\* ::= <exp> + <mulexp> | <mulexp> <mulexp> ::= <mulexp> \* <rootexp> | <rootexp> <rootexp> ::= let val <variable> = <exp> in <exp> end | (<exp>) | <variable> | <constant>

- A sample Language TWO expression:
   let val y = 3 in y\*y end
- What does the parse tree for the above expression look like?
- Notice that in TWO assignments are expressions and the variables bindings are only valid in the scope of the second expression of the let expression.

## TWO: Abstract Syntax

Additional abstract syntax nodes for language TWO:

- (1) var(X) dereferences a variable X
- (2) <u>let(X,E1,E2)</u> binds the variable X to expression E1 in the context of expression E2.

Example: the TWO program

let val y = 3 in y\*y end

will result in the AST

let(y,const(3),times(var(y),var(y)))

### From Parse Tree to Prolog AST

- Consider: 2 \* let x = 5 in 1+x end
  - Parse tree?
  - AST?
  - Prolog AST?

#### **TWO: Semantics**

In order to provide semantics we need to remember the values assigned to variables -- <u>binding environments</u> (fancy word for dictionary!)

In our case, for the Prolog based semantics, we let the terms bind(X,K) represent the binding of variable X to value K. A context is simply a list of these binding terms:

```
[bind(y,3),bind(q,20),bind(z,5)]
```

Given this binding structure, we can write a predicate, lookup/3, that returns a variable binding for a particular Var

```
lookup(Var,[bind(Var,Value)| _ ],Value).
lookup(Var,[ _ |Rest],Value) :- lookup(Var,Rest,Value).
```

Finds the most recent binding of variable Var if there is one.

#### **TWO: Prolog Interpreter**

val2(plus(X,Y),B,Value) :val2(X,B,XValue),
val2(Y,B,YValue),
Value is XValue + YValue.

val2(times(X,Y),B,Value) :val2(X,B,XValue),
val2(Y,B,YValue),
Value is XValue \* YValue.

val2(const(X),\_,X).

val2(var(X),B,Value) :lookup(X,B,Value).

```
val2(let(X,Exp1,Exp2),B,Value) :-
val2(Exp1,B,XValue),
val2(Exp2,[bind(X,XValue)|B],Value).
```

val2 / 3 - interpretation predicate first argument: AST second argument: binding env; third argument: semantic value.

#### Examples

```
let val y = 3 in y*y end
```

?- val2(let(y,const(3),times(var(y),var(y))),['],X).

X = 9

Yes

#### Exercises

- Use the semantics of TWO to show the following:
  - Assume that the context B = [bind(y,3)] then the semantic value of '2\*y' is 6
  - The semantic value of '2 \* let x = 3 in x \* x end' is 18

#### The semantic value of 'let x = 1 in let y = x + 1 in y end end' is 2



 Use the semantics to compute the meaning of the following expressions in TWO (use the rules given in the notes, the book has many typos):

```
1) let val y = 3 in 2*y end
```

```
2) let val y = 1 in
  let val y = 2 in
        y
        end
        end
```

Note: first construct an abstract syntax tree, then give the representation in Prolog notation, and then show the computation in our semantics.