Functional Programming

- Functional programming is defined by:
 - Programs exclusively consist of recursive definitions of functions
 - Everything is a value no statements allowed
 - We do allow:
 - Function definition statements (2)
 - Let statements for giving names to expressions
 - Return statements
 - Declarative approach to data via the use of pattern matching.
 - Functions as first-class citizens
 - This gives rise to higher-order programming.
- Functional Asteroid is called with '-F' switch
 - asteroid –F <program>

The Factorial Revisited

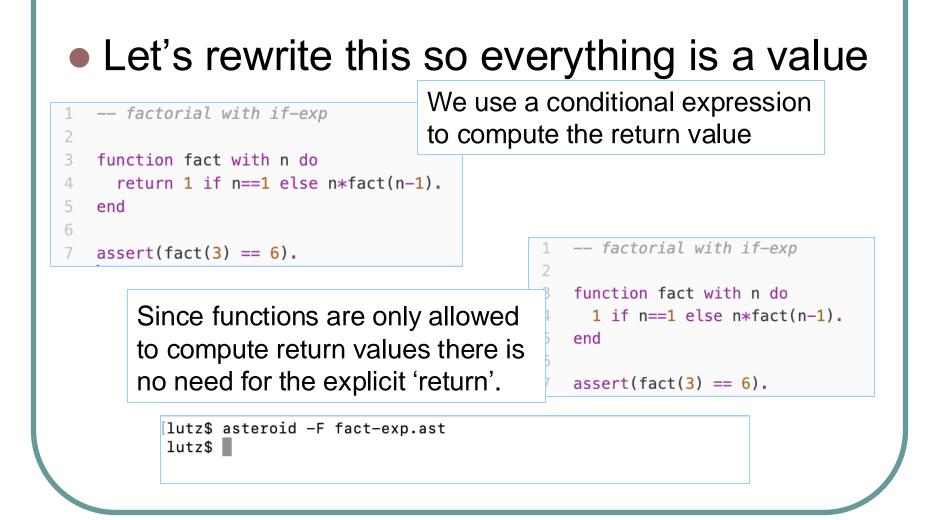
Let's start with something simple: Factorial

```
-- factorial with if-stmt
2
3
    function fact with n do
      if n == 1 do
4
        return 1.
5
6
     else
        return n * fact(n-1).
     end
9
    end
10
    assert(fact(3) == 6).
11
```

The problem is that if statements are not supported in the functional programming paradigm – they do not compute a value!

```
[lutz$ asteroid -F fact-stmt.ast
error: fact-stmt.ast: 4: if statement is not supported in functional mode
lutz$
```

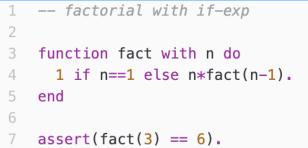
The Factorial Revisited





- SML is one of the classic functional languages next to Lisp.
- A web-based implementation of SML is available here,
 - https://sosml.org

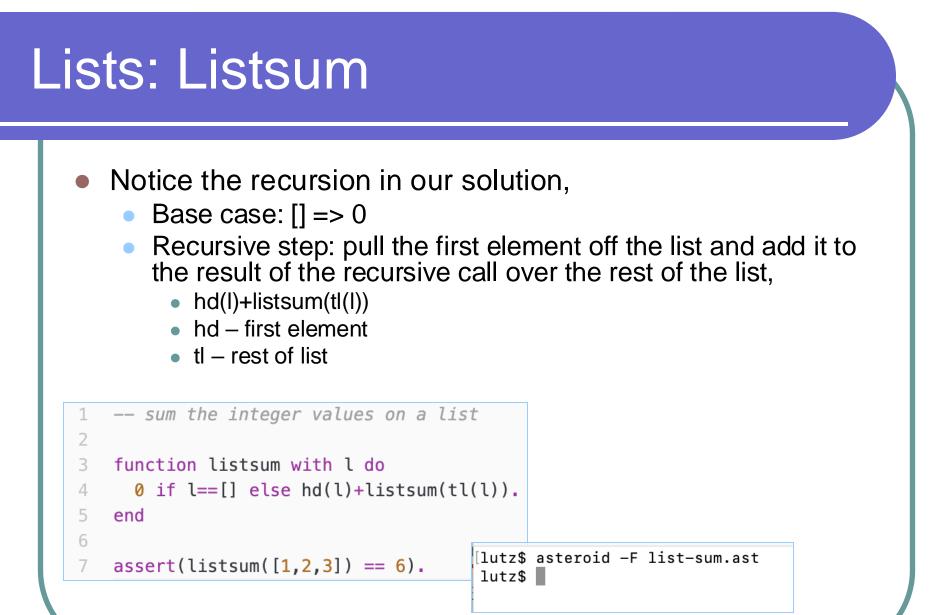
Asteroid



SML
(* factorial using if expression *)
fun fact n = if n=1 then 1 else n*fact(n-1);
fact(3) = 6;

Lists: Listsum

- Let's see how functional programming works with lists
 - Remember: no loops!
 - Everything has to be done with recursion
- Program: Assume we are given a list of integer values, sum all the integer values on the list. E.g. [1,2,3] => 6
- We need to use recursion.
 - Base case
 - Recursive step



SML & Listsum

Asteroid

2

4

6

7

```
-- sum the integer values on a list
function listsum with 1 do
0 if l==[] else hd(l)+listsum(tl(l)).
end
assert(listsum([1,2,3]) == 6).
               SML
            (* sum integer values on a list *)
            fun listsum l = if l=[] then 0 else hd(l)+listsum(tl(l));
            listsum([1,2,3]) = 6;
```

Class Exercise

• Write a program that given a list will count the number of elements on the list.

• E.g. [1,2,3] => 3, and [] => 0

 Write a program that given a list of integer values will return a list where each value on the list is double the value of the original value.

• E.g. [1,2,3] => [2,4,6], and [] => []

 All programs need to be written in functional Asteroid and need to be run with the '-F' flag in place.

Multi-Dispatch

- Since most functional programs consist of recursive functions all these functions will have a top-level 'if-else' expression to deal with the base vs recursive step.
- That style of programming gets tiring very fast and the code is not very readable.
- The solution: Multi-Dispatch
 - Introduce one function body for each of the steps.

Multi-Dispatch

Instead of this...

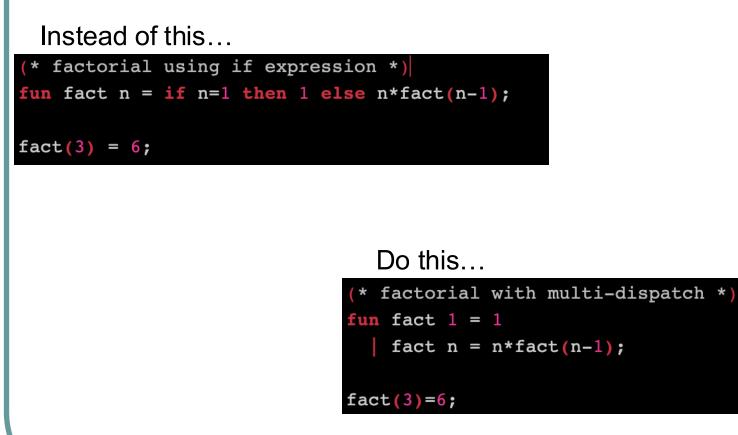
```
1 -- factorial with if-exp
2
3 function fact with n do
4 1 if n==1 else n*fact(n-1).
5 end
6
7 assert(fact(3) == 6).
```

Do this...

```
-- factorial with multi-dispatch
 2
3
    function fact
      with 1 do -- function argument == 1
4
 5
        1
      with n do -- function argument =/= 1
 6
7
        n*fact(n-1).
8
    end
9
10
   assert(fact(3) == 6).
```

Advantage: implicit testing or pattern matching of the function arguments!

Multi-Dispatch: SML



Multi-Dispatch

Instead of this...

```
1 -- sum the integer values on a list
2
3 function listsum with l do
4 0 if l==[] else hd(l)+listsum(tl(l)).
5 end
6
```

```
assert(listsum([1,2,3]) == 6).
```

Notice that we can pattern match on the structure of a list: E.g. []

Do this...

```
-- sum the integer values on a list
2
3
    function listsum
4
   with [] do
5
        0
6
     with l do
       hd(l)+listsum(tl(l)).
7
8
      end
9
    assert(listsum([1,2,3]) == 6).
10
```

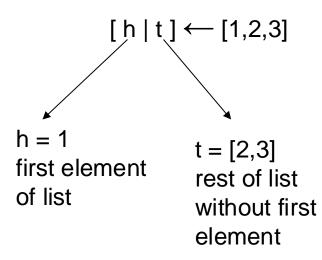
Pattern Matching

• In programming values have structure

- Lists are comprised of a sequence of elements
- Pairs are made up of two ordered values: first component and second component
- Integers are single values without a decimal part
- In pattern matching we state the expected structure of a value as a pattern possibly with variables
 - If the pattern matches the expected value, then we say that the pattern-match was successful, and variables will be bound to parts of the value that they matched.
 - Example: $(a,b) \leftarrow (1,2)$ with a=1 and b=2
 - Example: 1 ← 1

• Example: $x \leftarrow 3$ with x=3

 Instead of using 'hd' and 'tl' we can use pattern matching with the head-tail pattern '[h | t]'.



In listsum the head-tail pattern takes care of the analysis of the list!

Instead of this...

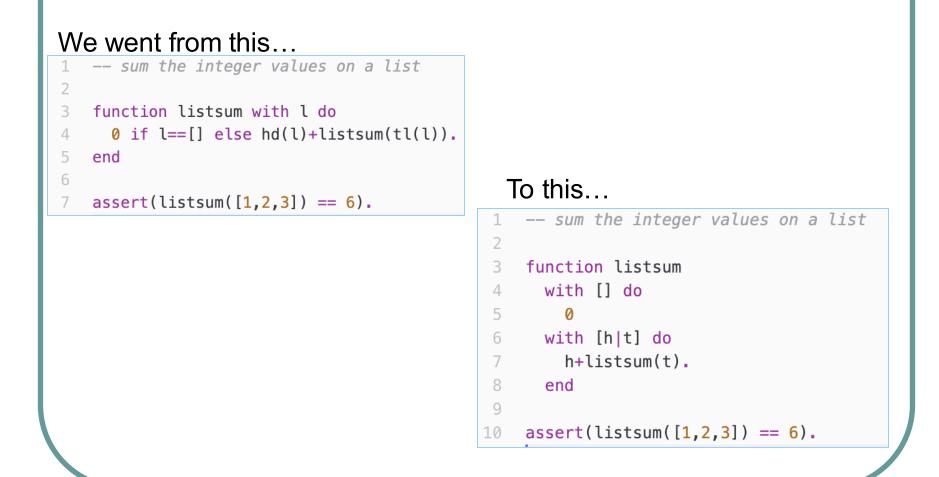
```
1 -- sum the integer values on a list
2
3 function listsum
4 with [] do
5 0
6 with l do
7 hd(l)+listsum(tl(l)).
8 end
9
10 assert(listsum([1,2,3]) == 6).
```

Do this...

```
1 -- sum the integer values on a list
2
3 function listsum
4 with [] do
5 0
6 with [h|t] do
7 h+listsum(t).
8 end
9
0 assert(listsum([1,2,3]) == 6).
```

- The hallmark of this multi-dispatch approach is that the interpreter does a lot of work for you for free:
 - It executes the body that matches the function argument
 - If the head-tail pattern matches the function argument it instantiates the first element in variable h and the rest of the list in variable t.

```
1 -- sum the integer values on a list
2
3 function listsum
4 with [] do
5 0
6 with [h|t] do
7 h+listsum(t).
8 end
9
10 assert(listsum([1,2,3]) == 6).
```



Head-Tail pattern matching is also available in SML

```
1 -- sum the integer values on a list
2
3 function listsum
4 with [] do
5 0
6 with [h|t] do
7 h+listsum(t).
8 end
9
10 assert(listsum([1,2,3]) == 6).
(*
11
```

```
(* listsum head-tail pattern matching *)
fun listsum [] = 0
        listsum (h::t) = h+listsum(t);
listsum([1,2,3])=6;
```

Head-Tail Pattern Matching: Python

Python also supports head-tail pattern matching...

```
Python 3.9.6 (default, Sep 13 2022, 22:03:16)
[Clang 14.0.0 (clang-1400.0.29.102)] on darwin
Type "help", "copyright", "credits" or "license" for more information.
>>> (h,*t) = [1,2,3]
>>> h
1
>>> t
[2, 3]
>>>
```

Functional Style Programming in Python

- A recursive program with pattern matching in Python
- Functional programming is more explicit about the intentions of a program
- This is often called declarative programming
- Functional and logic programming are considered declarative programming paradigms

```
def listsum(l):
    acc = 0
    for v in l:
        acc += v
    return acc
assert(listsum([1,2,3]) == 6)
```

Imperative Programming

```
def listsum(l):
  match l:
    case [] :
        return 0
        case (h,*t) :
        return h+listsum(t)
assert(listsum([1,2,3]) == 6)
```

Functional Programming

Wildcard Pattern

 If we need to match a value but we don't care what that value is, we can use a wildcard pattern '_'

```
-- wild card pattern
2
3
   function zero
     with 0 do
4
     "zero"
5
     with _ do -- wild card
       "something else"
7
   end
9
   assert(zero(0) == "zero").
   assert(zero(1) == "something else").
```

```
-- wild card pattern in structures
   function pair
3
     with (1,1) do
4
       "pair with two ones"
5
     with (a,_) do -- wild card within structure
6
       "pair with first component: "+a
     with do
       "not a pair"
9
0
   end
   assert(pair (1,1) == "pair with two ones").
   assert(pair (3,4) == "pair with first component: 3").
   assert(pair (1,2,3) == "not a pair").
```

Type Patterns

- Type patterns match all the values of a particular type.
- Type patterns are written with the '%' followed by the type name.
- A type pattern that matches all integer values is %integer.
- Type patterns can appear anywhere where patterns can appear.
- All built-in types are supported: %integer, %real, %string, %list, %tuple, %boolean
- User defined type patterns are %<name of the structure>.
 - For example if you created a structure called MyStruct then the associated type pattern is %MyStruct and will only match objects instantiated from MyStruct

```
-- a function that determines whether a value
   -- is an integer value or not
  function isinteger
4
5
   with %integer do
6
       true
7
    with do
       false
    end
   assert(isinteger(1) == true).
11
   assert(isinteger(1.0) == false).
12
```

Conditional Patterns

- We can limit the values that a variable can match by using a special conditional pattern: <var> : <pattern>
 - x:%real states that 'x' can only match floating point values.
 - q:(%integer,%integer) states the 'q' can only match pairs of integer values.

```
-- the typed version of factorial
 1
     -- factorial is only defined over the integers
 2
 3
      load system io.
 4
 5
 6
      function fact
 7
         with 1 do
 8
            1
         with n:%integer do
 9
            n*fact(n-1)
10
        with _ do
11
            throw Error "not an integer value".
12
13
      end
14
15
     assert(fact(3) == 6).
16
     try
         fact(3.0)
17
18
      catch s do
         io @println s. -- catch the error
19
20
      end
```

Structural Patterns

- Structural patterns means pattern matching on structure in addition to values.
- On the previous slide we saw one instance of that:
 - (%integer,%integer) match pairs of integer values.

Structural Patterns

 The empty list '[]', single element list '[e]', and the head-tail pattern '[x|y]' are also structural patterns...

function halve
with [] do
([],[])
with [a] do
([a],[])
with [a b rest] do
<pre>let (llist,rlist) = halve(rest).</pre>
<pre>([a]+llist,[b]+rlist)</pre>
end

Here [a | b | rest] is the same as [a | [b | rest]].

Structural Patterns

We can nest arbitrary structures as patterns...

```
function merge
with ([],rlist) do
rlist
with (llist,[]) do
llist
with ([a]llist],[b]rlist]) do
[a]+merge(llist,[b]+rlist) if a < b
else [b]+merge([a]+llist,rlist)
end</pre>
```

Patterns & Let

- Even though the 'let' statement looks like an assignment statement it is actually a pattern-match statement of the form,
 - let <pattern> = <value>
- It takes the value on the right and pattern-matches it against the pattern on the left.
- If the pattern contains variables, they will be instantiated in the current namespace.
- All patterns we have discussed so far are also valid as let statement patterns

```
1 -- examples of the let statement
2
3 let x = 1. -- the variable x is the simplest pattern possible
4 let 1 = 1. -- the 1 on the left is the pattern, on the right the value
5 let x:%integer = 1. -- type patterns work here too
6 let (x,y) = (1,2). -- pattern instantiated x=1 and y=2
7 let ((a,b),(c,d)) = ((1,2),(3,4)). -- pair of pairs
8 let [a|b] = [1,2,3]. -- head-tail pattern match
```

The MergeSort

1 2

3

4 5

6

7

8

9

10 11

12

13

14 15

16 17

18 19

20

22

21

23

24

25

26

27

28

29

30 31

32 33

 Putting this all together – the MergeSort

```
-- the mergesort
load system io.
function mergesort
   with [] do
      []
   with [a] do
      [a]
   with l do
      function halve
         with [] do
            ([], [])
         with [a] do
            ([a],[])
         with [a|b|rest] do
            let (llist,rlist) = halve(rest).
            ([a]+llist,[b]+rlist)
      end
      function merge
         with ([],rlist) do
            rlist
         with (llist,[]) do
            llist
         with ([a|llist],[b|rlist]) do
            [a]+merge(llist,[b]+rlist) if a < b</pre>
               else [b]+merge([a]+llist,rlist)
      end
      let (x,y) = halve(1).
      merge(mergesort(x),mergesort(y)).
end
io @println(mergesort([3,2,1,0])).
```

Reading

Asteroid User Guide

Functions

• https://asteroid-lang.readthedocs.io/en/latest/User%20Guide.html#functions

Pattern Matching

https://asteroid-lang.readthedocs.io/en/latest/User%20Guide.html#pattern-matching

Assignment

Assignment #3 – see BrightSpace